Stacks, Queues & Trees

Prof. Dr. Harald Gall Institut für Informatik Universität Zürich http://seal.ifi.uzh.ch





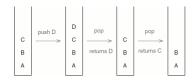
The Stack Interface

- Stack
 - Data structure holding several items.
 - New items added to the top of the stack.
- Pushing
 - Push items onto the stack
- Pop
 - Pop items off of the stack or extract the topmost item.
- Peek
 - Peek at the top item or check if the stack is empty.



The Stack Interface

- last-in, first-out or LIFO policy
 - Last item pushed on the stack is next item popped off the stack



_			
MA	University	of	Zurich

The Stack Interface 1 /** A last-in, first-out stack of Objects. */ 2 public interface Stack { 3 4 /** Return true if this Stack is empty. */ 5 public boolean isEmpty(); 6 6 7 /** 8 * Return the top Object on this Stack. Do not modify the Stack. 9 * @throws EmptyStructureException if this Stack is empty. 10 */ 11 public Object peek();

University of Zurich

The Stack Interface

```
13 /**
14 * Remove and return the top Object on this Stack.
15 * @throws EmptyStructureException if this Stack is empty.
16 */
17 public Object pop();
18
19 /** Add target to the top of the Stack. */
20 public void push(Object target);
21
22}
```

University of Zurich

The Stack Interface

- Generics
 - The Stack interface describes a stack of Objects.
 - s.push(new Die(3));
 - When we pop a Stack we get back an Object.
 - We usually cast it to a more specific class so we can use specific functionality.
 - ((Die)(s.pop())).roll();
 - This is not only inconvenient, it is slightly unsafe.
 - We must remember what we put on the Stack, or we might try to cast something that is not really a Die to be a Die.



The Stack Interface

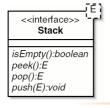
- Generic classes and interfaces
 - Has one or more *type parameters*.
 - We have to specify a type for each type of parameter.
 - Stack<Die> s = new Stack<Die>():
 - s.push(new Die());s.pop().roll();
 - Java won't let us push anything of the wrong type onto this Stack.
 - The pop() method's return type is specified by the type parameter.



The Stack Interface

The Stack Interface

 In UML diagrams type parameters are shown as dashed boxes are at the upper right of a class.



University of Zurich

The Call Stack 1 /** Compute the hypotenuse of a right triangle. */ 2 public class Hypotenuse { 3 4 /** Return the square of the number x. */ 5 public static double square(double x) { 6 return x * x; 7 } 8 9 /** 10 * Return the hypotenuse of a right triangle with side lengths x 11 * and y. 12 */ 13 public static double hypotenuse(double x, double y) {

The Call Stack

University of Zurich

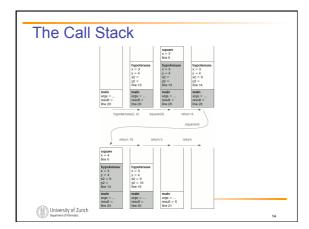
- The hypotenuse() method invokes the square() method twice.
- How does Java know where to go when it finishes an invocation of square()?
- Java keeps track of what it was doing before the invocation started by using a stack.
 - This stack is called a call stack.

(CHIN	University of Zurich
E 1111 27	
	Department of Informatics

The Call Stack

- Every time a method is invoked, a call frame is created.
 - The call frame keeps track of the current state of the method.
 - It stores any arguments or variables for the method.
 - It also keeps track of how far along the method has proceeded.





The Call Stack

- Knowledge of the call stack helps us understand some of Java's error messages.
- The error message shows a stack trace (a snapshot of the call stack) indicating what was going on when the program crashed.

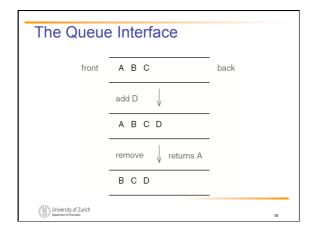


The Call Stack 1 Exception in thread "main" 2 java.lang.ArrayIndexOutOfBoundsException: -1 3 at Deck.deal(Deck.java:25) 4 at IdiotsDelight.deal(IdiotsDelight.java:24) 5 at IdiotsDelight.play(IdiotsDelight.java:58) 6 at IdiotsDelight.main(IdiotsDelight.java:81)

The Queue Interface

- Queue
 - Very similar to a stack.
 - Items are inserted in one end (the back) and removed from the other end (the front).
 - first-in, first-out, or FIFO





The Queue Interface 1/** A first-in, first-out queue of Objects. */ 2 public interface Queue
 3 4 /** Add target to the back of this Queue. */ 5 public void add(E target); 6 7 /** Return true if this Queue is empty. */ 8 public boolean isEmpty(); 9 10 /** 11 * Remove and return the front item from this Queue. 12 * @throws EmptyStructureException if the Queue is empty. 13 */ 14 public E remove(); 15 16}

Ordered Lists

University of Zurich Department of Informatics

- Since a Set changes size as items are added and removed, a linked structure seems in order.
- An OrderedList is like a LinkedList, except that:
 - The elements of an OrderedList must implement the Comparable interfaces
 - The elements of an OrderedList are kept in order.
 - The OrderedList class implements the Set interface.
 It provides the methods add(), contains(), remove(), and size(). No duplicate elements are allowed.

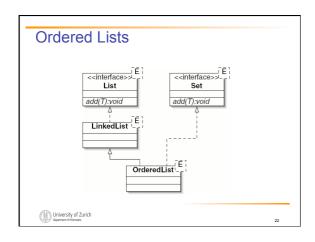


20

Ordered Lists

- Extending LinkedList
 - The problem is that the LinkedList class implements the List interface, which conflicts with the Set interface.
 - The add() method from the List interface should add the argument target to the end of the list, even if it is already present, while the add() method from the Set interface may add target at any position, but not if it is already present.

University of Zurich Department of Informatics



Ordered Lists 1 /** A linked list of Comparable items, in increasing order. */ 2 public class OrderedList< extends Comparable<.>> 3 implements Set<.>>, Predecessor<.>> { 4 5 /** The first node in the list. */ 6 private ListNode<.> front; 7 University of Zurich Represed Forman. 23

```
Ordered Lists

8  /*An OrderedList is initially empty. */
9  public OrderedList() {
10  front = null;
11  }
12  public ListNode<E> getNext() {
14  return front;
15  }
16  17  public void setNext(ListNode<E> next) {
18  front = next;
19  }
20  21  public int size() {
21  int tally = 0;
22  for (ListNode<E> node = front;
24  node != null;
25  node = node.getNext()) {
26  tally++;
27  }

University of Zurich
Department of theresion

24
```

Ordered Lists

```
return tally;

public String toString() {
    String result = "(";
    for (ListNode<E> node = front;
    node != null;
    node = node.getNext()) {
    result += node.getItem() + "";
    }
} return result + ")";
}

du
```

University of Zurich

25

Ordered Lists

- To add something to a Set, we must first find where it belongs, then (if it is not present) put it there.
- To remove something, we must first find where it belongs, then (if it is present) remove it.
- Since the final "put it there" and "remove it" operations take constant time, all three methods have the same order of running time for a given implementation.

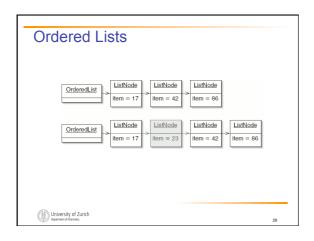


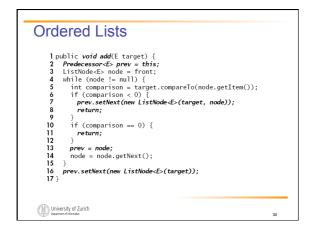
Ordered Lists

• The contains() method for the OrderedList class is a linear search.

University of Zurich

```
I public boolean contains(E target) {
2  ListNode<E> node = front;
3  while (node != null) {
4  int comparison = target.compareTo(node.getItem());
5  if (comparison < 0) {
6   return false;
7  }
8  if (comparison == 0) {
9   return true;
10  }
11  node = node.getNext();
12  }
13  return false;
14}
University of Zurich
Supermed Vibration</pre>
```





Ipublic void remove(E target) { Predecessor<E> prev = this; ListNode<E> node = front; while (node != null) { int comparison = target.compareTo(node.getItem()); if (comparison < 0) { return; } if (comparison = 0) { prev.setNext(node.getNext()); return; } prev = node; node = node.getNext(); } } </pre>

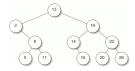
Ordered Lists

 The OrderedList data structure is easy to implement, but it requires linear time for search, insertion, and deletion.

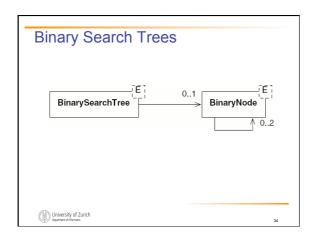


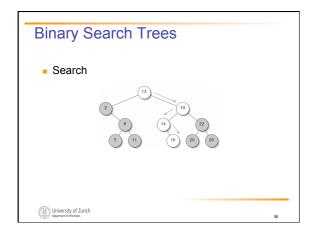
Binary Search Trees

- Binary search tree
 - More efficient under some circumstances.



University of Zurich
Department of Informatics





I public boolean contains(E target) { BinaryNodecEs node = root; while (node! = null) { int comparison = target.compareTo(node.getItem()); if (comparison < 0) { // Go left node = node.getLeft(); } else if (comparison == 0) { // Found it return true; } else { node = node.getRight(); } } else { node = node.getRight(); } return false; } **University of Zurich** **Unive

Binary Search Trees

- Searching a binary search tree.
 - In a perfect tree, this is $\Theta(\log n)$
 - In the Anagrams program when the word file is in alphabetical order, it produces a worst case. Every new node is a right child.



Binary Search Trees Insertion Jay 19 Binary Search Trees Insertion Jay 19 Jay 19

Binary Search Trees

- There are two complications to the code:
 - Once we reach a null node, we have forgotten how we got there. Since we need to modify either the left or right field in the parent of the new leaf, we'll need this
 - We need to deal with the situation in which the binary search tree is empty.



Binary Search Trees

```
1 /**
2 * Something which has children, such as a BinarySearchTree or a
3 * BinaryNode.
4 */
5 public interface Parent<E> {
6 /**
8 * Return the left child if direction < 0, or the right child
9 * otherwise.
10 */
1 public BinaryNode<E> getChild(int direction);
12
14 * Replace the specified child of this parent with the new chil
5 * If direction < 0, replace the left child. Otherwise, replac
6 * the right child.
7 */
18 public void setChild(int direction, BinaryNode<E> child);
19
20}
                       * Replace the specified child of this parent with the new child.
* If direction < 0, replace the left child. Otherwise, replace
* the right child.
```

University of Zurich

Binary Search Trees

```
lpublic BinaryNode<E> getChild(int direction) {
2  if (direction < 0) {
3    return left;
4  } else {
5    return right;
6  }
7}</pre>
7 }
8 
9 public void setChild(int direction, BinaryNode<E> child) {
10 if (direction < 0) {
11 left = child;
12 } else {
13 right = child;
14 }
15}</pre>
```

University of Zurich

Binary Search Trees

```
1 public BinaryNode<E> getChild(int direction) {
2   return root;
3 }
4
5 public void setChild(int direction, BinaryNode<E> child) {
6   root = child;
7 }
```

University of Zurich

43

Binary Search Trees

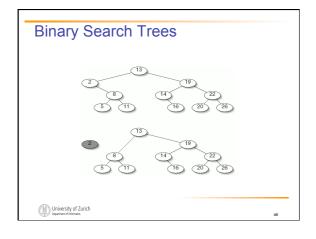
University of Zurich

44

Binary Search Trees

- Deletion
 - The challenge is to make sure the tree is still a binary search tree when we're done with the deletion.
 - Deleting a leaf, this is easy.
 - If the node has only one child, we just splice it out much as we would a node in a linked list.

University of Zurich



Binary Search Trees

- When the node we want to delete has two children.
 - We must be very careful about which node we choose to delete so that the tree will still be a binary search tree.
 - It is always safe to choose the inorder successor of the node we originally wanted to delete.
 - Find a node's inorder successor by going to the right child, then going left until we hit a node with no left child.
 - It can have a right child.



Binary Search Trees

- It is safe to replace the node we want to delete with its inorder successor.
 - It is therefore larger than anything in the left subtree and smaller than anything else in the right subtree.



Binary Search Trees direction = comparison; University of Zurich Department of Informatics

Binary Search Trees $1/^{\pm x}$ 2 * Remove node, which is a child of parent. Direction is positive 3 * if node is the right child of parent, negative if it is the 4 * left child. 5 */ University of Zurich

Binary Search Trees

- We don't need special code for the case where node is a leaf, because in this situation parent.setChild(direction, node.getRight());
- Is equivalent to:
 - parent.setChild(direction, null)



binary Search Trees 1 /** 2 * Remove the leftmost descendant of node and return the 3 * item contained in the removed node. 4 */ 5 protected E removeLeftmost(BinaryNode<E> node, Parent<E> parent) { 6 int direction = 1; 7 while (node.getLeft()!= null) { 8 parent = node; 9 direction = -1; 10 node = node.getLeft(); 11 } 12 E result = node.getItem(); 13 spliceOut(node, parent, direction); 14 return result; 15}

Binary Search Trees

- BinarySearchTrees should not be used in the plain form explained here.
 - The worst-case, running time is linear
 - Worst case are not uncommon.

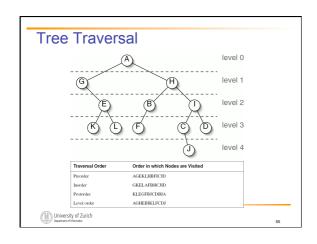


University of Zurich

Tree Traversal

- Four meaningful orders in which to traverse a binary tree.
 - Preorder
 - Inorder
 - Postorder
 - Level order





Tree Traversal 1 /** 2 * Return a String representation of the tree rooted at this node, 3 * traversed preorder. 4 */ 5 public String toStringPreorder() { 6 String result = ""; 7 result += item; 8 if (left != null) { 9 result += left.toStringPreorder(); 10 } 11 if (right != null) { 12 result += right.toStringPreorder(); 13 } 14 return result; 15}

```
Tree Traversal

1 /**
2 * Return a String representation of the tree rooted at this node,
3 * traversed inorder,
4 */
5 public String toStringInorder() {
6 String result = "";
7 if result = "left.toStringInorder();
9 }
10 result == ifee;
11 if (right != null) {
12 result == right.toStringInorder();
13 }
14 return result;

15}

University of Zurich Representations
```

Tree Traversal 1 /** 2 * Return a String representation of the tree rooted at this node, 3 * traversed postorder. 4 // 5 public String toStringPostorder() { 6 String result = ""; 7 if (left |= null) { 8 result += left.toStringPostorder(); 9 } 10 if (right != null) { 11 result += right.toStringPostorder(); 12 } 13 result += item; 14 return result; 15} University of Zurich Departed vibration.

```
Tree Traversal

1 /**

2 * Return a String representation of the tree rooted at this node,
3 * traversed level order.
4 */
5 public String toStringLevelOrder() {
6 String result = "";
7 Queue-BinaryNode-E>> q = new ArrayQueue-BinaryNode-E>>();
8 q.add(this);
9 while (!(q.isEmpty())) {
10 BinaryNode-E> node = q.remove();
11 result += node.item;
12 if (node.left != null) {
13 q.add(node.left);
14 }
15 if (node.right != null) {
16 q.add(node.right);
17 }
18 }
19 return result;
20}

University of Zunich
Descreed Horses.
```

Tree Traversal

- Level order traversal is sometimes called breadthfirst.
- The other traversals are called *depth-first*.
- \blacksquare Traversal takes $\Theta(n)$ in both breadth-first and depth-first.
- Memory usage in a perfect tree is ⊕(log n) in depth-first and ⊕(n) in breadth-first traversal.



General Trees

- General Tree
 - General trees differ from binary trees in three ways:
 - A node in a general tree may have more than two children.
 - General trees cannot be empty. This restriction is made to avoid having to distinguish between a node with no subtrees and a node with several empty subtrees, which would be drawr identically.

University of Zurich

General Trees

- A node in a general tree has a (possibly empty) sequence of children, rather than a certain number of "slots" to fill.
- Binary trees
 - a tree with a left subtree but no right subtree
 - a tree with a right subtree but no left subtree.
- No such distinction is made for general trees





University of Zurich

General Trees

• Inheritance diagrams showing the relationships between classes is a general tree.



University of Zurich

General Trees

- Simplest is to represent each node as an item.
 - Array of children or list of children.
 - First-child, next-sibling
 - A less intuitive but more space-efficient representation has each node keeping track of its first child and its next sibling.



